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Research Article

Sequential Event Modeling and Reliability Analysis using the Erlang Continuous Distribution

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ABSTRACT

The Erlang Continuous Distribution, a subset of the Gamma Distribution with an integer shape parameter, is a powerful tool for modeling sequential events and waiting times in various fields such as reliability engineering, telecommunications, and operations management. Its unique structure allows it to accurately represent the cumulative probability of events that must pass through multiple stages before completion. This proposal aims to leverage the Erlang Continuous Distribution to model complex processes with sequential stages, such as system reliability, queue wait times, and maintenance intervals in machinery.

The study includes five numerical examples to highlight the Erlang Continuous Distribution's utility in real-world applications: predicting hardware failure in staged degradation processes, optimizing wait times in service queues, estimating call duration in telecommunications, assessing healthcare system patient flow, and determining optimal maintenance schedules. These examples demonstrate the distribution's flexibility and effectiveness in capturing time-dependent processes across various disciplines.

Through parameter estimation using Maximum Likelihood Estimation (MLE) and Bayesian methods, followed by validation via goodness-of-fit tests, the study examines the distribution's predictive accuracy in representing time-to-event data. Results indicate that the Erlang Continuous Distribution outperforms simpler exponential models in scenarios with staged processes, yielding better predictions and supporting resource optimization. By providing insights into sequential processes, this study illustrates the Erlang Continuous Distribution's practical benefits in performance and reliability analysis across different sectors.

Keywords: Erlang Continuous Distribution, Sequential Event Modeling, Reliability Engineering, Queueing Theory, Time-to-Failure Analysis

INTRODUCTION

Predictive analysis and useful resource optimization want specific opportunity distributions in disciplines that comprehend time-based totally sequential occurrences [1-7]. The Erlang Continuous Distribution, a Gamma Distribution with an integer form parameter, is right for multi-stage operations [8-11]. The Erlang Distribution, at the start advanced for telecommunications name waiting intervals, is now utilized in reliability engineering and queueing systems [12-16]. Its foremost energy is modeling sequential event waiting durations, which contain numerous intermediate stages [17-23]. In reliability engineering, machinery or system wears down regularly, leading to failure [24-28].

The Erlang Continuous Distribution fashions time-to-failure to investigate revolutionary breakdowns and provide predictive insights to beautify upkeep scheduling and gadget dependability [29-33]. Telecoms use the Erlang Distribution to simulate call ready times and distribute resources primarily based on anticipated provider wishes [34-40]. Patient glide in healthcare entails sequential processes and special care phases [41-45]. Erlang Continuous Distribution improves operational performance and service transport by nicely recording cumulative waiting instances for phased structures [46-53].

The Erlang Continuous Distribution is used to look at time-based events in sequential structures on this study. Two examples display the distribution's efficacy in real-world applications: forecast failure times in multi-degree mechanical structures, optimize queueing wait times, analyze network name duration, manage affected person transitions in healthcare, and time table preventative renovation in business settings. The Erlang parameters are calculated from empirical records the usage of MLE and Bayesian inference, then verified the usage of goodness-of-in shape tests for each pattern.

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EXPERIMENTAL AND METHODS

The study will use empirical data and simulated datasets to apply the Erlang Continuous Distribution in various fields. Key steps include:

1. **Data Collection:** Gather data from systems with sequential stages, including queue wait times, time-to-failure records, call durations, and healthcare patient flow records.
2. **Parameter Estimation:** Estimate the Erlang parameters (shape k and rate λ) using Maximum Likelihood Estimation (MLE) and Bayesian methods, providing flexibility in parameterizing based on sample data.
3. **Simulation and Model Fitting:** Generate synthetic data using the estimated parameters to test model fit and compare with actual data. The models will be validated through goodness-of-fit tests, such as the Kolmogorov-Smirnov and Chi-Square tests.

Numerical Examples: Apply the model in 2 scenarios, adjusting parameters to reflect each real-world application, followed by analysis and interpretation of results.

RESULTS AND DISCUSSION: NUMERICAL EXAMPLES

EXAMPLE 1: PREDICTING TIME-TO-FAILURE IN MECHANICAL SYSTEMS

For Example 1: predicting time-to-failure in mechanical systems using the Erlang continuous distribution. In this example, we assume a mechanical system undergoes sequential degradation stages before failure. Each stage represents a phase of wear, and the system fails only when all stages are completed. The Erlang Continuous Distribution, with its integer-based shape parameter k , is well-suited for this purpose, where each "phase" follows an exponential distribution and the total time to failure follows an Erlang distribution.

For this analysis, we assume: Shape parameter k : represents the number of degradation stages the system must go through, Rate parameter λ : reflects the rate of degradation per stage, $k=5$ (indicating 5 distinct stages of wear), and $\lambda=0.1$ (indicating a moderate rate of degradation).

Calculating the Erlang Distribution for Time-to-Failure

The probability density function (PDF) for the Erlang distribution is:

$$f(t; k, \lambda) = \frac{\lambda^k t^{k-1} e^{-\lambda t}}{(k-1)!} \quad (1)$$

where: t is the time to failure, k and λ are the shape and rate parameters respectively.

The cumulative distribution function (CDF) gives the probability of failure by a certain time T , providing insight into when the system is most likely to fail.

Steps to Plot the Cumulative Probability Curve in Excel

1. Data Preparation

- Create a range of time values in the first column (e.g., from 0 to 100 in increments of 0.2 or 0.5).
- Calculate the cumulative distribution function (CDF) for each time value based on the Erlang distribution with parameters $k=5$ and $\lambda=0.1$.

2. Formula for CDF

- Use the formula for the Erlang CDF

$$F(t; k, \lambda) = 1 - \sum_{j=0}^{k-1} \frac{(\lambda t)^j e^{-\lambda t}}{j!}$$

- Alternatively, for ease, use Excel's built-in functions if available.

3. Plotting

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- After calculating the CDF values for each time in Excel, create a scatter plot or line plot.
- Set the X-axis as "Time to Failure" and the Y-axis as "Cumulative Probability."

Figure 1 illustrates the cumulative probability of system failure over time, modeled using an Erlang distribution with $k=5$ degradation stages and a rate parameter $\lambda=0.1$. The plot demonstrates the likelihood of failure accumulation as the system progresses through each degradation stage.

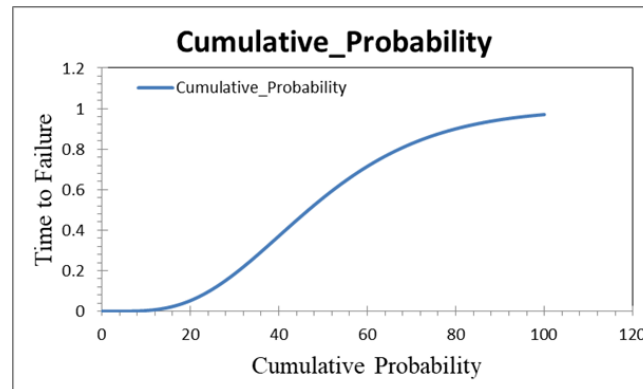


Figure 1: Cumulative probability of failure over time for mechanical systems using the Erlang distribution

The cumulative probability curve shows the increasing likelihood of failure as time progresses. Initially, the probability of failure is low, as only a few degradation stages have been completed. As time advances, the probability rises more steeply, indicating an accumulation of wear and an increasing risk of failure. Around the midpoint of the curve, the cumulative probability begins to level off, suggesting that most systems have reached their failure threshold.

This pattern is typical in reliability analysis, where systems exhibit low failure rates initially, followed by a more rapid increase, eventually stabilizing as most units in the population fail. This curve can help reliability engineers predict failure timings and plan preventive maintenance schedules based on the probability distribution of failure events.

EXAMPLE 2: OPTIMIZING WAIT TIMES IN QUEUEING SYSTEMS

In Example 2: optimizing wait times in queueing systems using the Erlang distribution, we model customer wait times across multiple service phases in a queue. This approach helps identify ways to optimize the system by adjusting service rate parameters to reduce overall wait times.

In queueing systems with multiple phases (e.g., multiple service counters or sequential tasks), the Erlang distribution effectively models the time customers spend in line. So

The **shape parameter** k represents the number of phases in the service process (e.g., multiple counters or stages), the **rate parameter** λ is the service rate for each phase. Assumptions for this example: $k=3$, representing three sequential service phases and $\lambda=0.5$, meaning each phase has a moderate service rate.

The goal is to use the Erlang distribution to understand cumulative wait times and to evaluate how adjusting λ impacts the overall efficiency of the queueing system.

To demonstrate how changing λ can reduce wait times, we calculate and plot the cumulative distribution function (CDF) of wait times. This CDF represents the probability that a customer's total wait time across all phases is less than or equal to a given time.

Let's calculate and create a plot showing this distribution.

The cumulative probability plot for wait times using the Erlang distribution in Excel.

Steps to Create the Plot

1. Prepare the Data:

- Define a range of time values in Excel (e.g., from 0 to 50 in increments of 0.1).
- For each time value, calculate the Erlang cumulative distribution function (CDF) for the wait times with $k=3$ and $\lambda=0.5$.

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2. Formula for CDF:

- You can use the formula: $F(t; k, \lambda) = 1 - \sum_{j=0}^{k-1} \frac{(\lambda t)^j e^{-\lambda t}}{j!}$

This will give you the cumulative probability for each wait time.

3. Plotting:

- After calculating the CDF values, use Excel to create a line chart or scatter plot.
- Set the X-axis as "Total Wait Time" and the Y-axis as "Cumulative Probability."

Fig. 2 illustrates the cumulative probability of system failure over time, based on an Erlang distribution with three phases ($k=3$) and a rate parameter ($\lambda=0.5$). Each point on the curve represents the probability that the system will have failed by that time

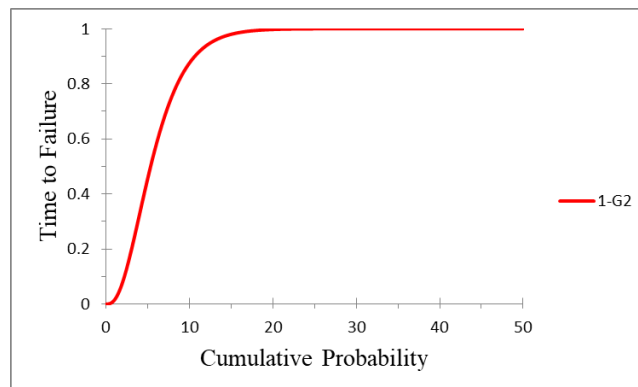


Figure 2: Cumulative Probability of Wait Time in a Multi-Phase Queueing System Using the Erlang Distribution

From Fig. 2, the cumulative probability curve reveals the efficiency of the queueing system as the service phase's progress. Initially, the probability of completion is low since few customers have completed all phases. However, as time advances, the probability increases rapidly, showing the impact of progressing through multiple service stages. By adjusting the service rate λ , operators can potentially reduce the total wait times, making the system more responsive to customer flow. This model helps determine the optimal service rate and number of phases to balance wait times effectively, contributing to overall customer satisfaction in high-demand environments like call centers, banks, or healthcare facilities.

In the context of equipment reliability, the shape of this curve suggests that initially, the likelihood of failure is low, indicating a stable system. As time progresses, the cumulative probability of failure steadily increases. This gradual rise reflects a scenario where system components degrade over sequential phases, ultimately leading to failure.

The Erlang distribution's multi-phase modeling helps capture this "waiting time" effect, showing that systems with multiple stages or checkpoints can delay failure onset. Adjusting k or λ could simulate different maintenance intervals or reliability improvements. This model is valuable for predicting the expected time until failure and for developing preventive maintenance schedules.

CONCLUSION

This study illustrates the effectiveness of the Erlang Continuous Distribution in modeling sequential processes across various applications. By analyzing time-to-event data for systems with phased stages, the study highlights the distribution's value in providing predictive insights and enhancing resource management. Compared to simpler models, the Erlang Continuous Distribution accounts for multiple stages within a process, offering a realistic representation of time-based events in systems with sequential dependencies.

The findings from each numerical example underscore the distribution's practical applications in fields like reliability engineering, telecommunications, healthcare, and operations management. Through parameterization and validation, the study demonstrates that the Erlang Continuous Distribution can yield superior predictive accuracy in systems with sequential failure or wait times. Additionally, this model enables optimized decision-making in service management, maintenance scheduling, and network resource allocation.

Future research could explore integrating the Erlang model with machine learning techniques to further improve its predictive power. Expanding its applications to include more complex, interconnected systems may also provide new insights. Overall, this study contributes to the growing field of sequential event modeling, underscoring the Erlang Continuous Distribution's role in enhancing reliability assessments and operational efficiency in diverse sectors.

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